

Programming Languages

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Roadmap

- Creating Language Grammars
 - Regular Expressions
 - Context Free Grammars
 - Parse Trees
 - Ambiguity



Expressing Digits

digit -> 0
digit -> 1
digit -> 2
digit -> 3
digit -> 4
digit -> 5
digit -> 6
digit -> 7
digit -> 8
digit -> 9

digit -> 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

Regular Expression

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Expressing Numbers

digit -> 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

two-digit-number -> digit digit

number -> digit digit*

* : Kleene star (zero more repetitions of the symbol to its left)

natural_number -> non_zero_digit digit*

non_zero_digit -> 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9

Non-terminals

Terminals

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Operators

- $op \rightarrow + \mid - \mid * \mid /$
- $expr \rightarrow \text{number } op \text{ number } op \text{ number}$

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Context Free Grammars

- Adds recursion to regular expressions

$expr \rightarrow \text{number } op \text{ number } op \text{ number}$

$expr \rightarrow \text{number} \mid expr \text{ } op \text{ } expr$

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Example

$3 + 4 * 5$ ← derive this

$\text{expr} \rightarrow \text{number} \mid \text{expr op expr}$

← from this

$\text{expr} \rightarrow \text{expr op expr}$
 $\rightarrow \text{expr op number}$
 $\rightarrow \text{expr} * \text{number}$
 $\rightarrow \text{expr op expr} * \text{num}$
 $\rightarrow \text{expr op num} * \text{num}$
 $\rightarrow \text{expr} + \text{num} * \text{num}$
 $\rightarrow \text{num} + \text{num} * \text{num}$
 (3) (4) (5)